

Listing of Claims:

1. (Currently Amended) An asymmetrical cryptographic method ~~of~~ for protecting a hard-wired electronic logic chip against fraud in transactions between the electronic chip and an application, including calculating an authentication value V from input parameters in the electronic chip, said method comprising the steps of:

producing a pseudo-random number r at the application prior to a transaction;

calculating a corresponding parameter x at the application prior to the transaction, said parameter x being linked to the pseudo-random number r by a mathematical relationship;

storing the parameter x in a data memory of the electronic chip prior to the transaction;

[[- 1)]] producing, at the chip, ~~producing a~~ the pseudo-random number r specific to the transaction ~~by means of~~ via a serial pseudo-random generator included in the chip, said chip reading the stored parameter x calculated by the application prior to the transaction;

[[- 2)]] sending from the chip ~~sending to~~ the application [[a]] the parameter x calculated by the application prior to the transaction, which is linked to the ~~random~~ pseudo-random number r by [[a]] the mathematical relationship[[.]] and stored in [[a]] the data memory of the chip[[.]];

[[- 3)]] calculating, at the chip, ~~calculating~~ a parameter y constituting the ~~whole~~ an entire or a portion of the authentication value V ~~by means of~~ via a serial function whose input parameters are at least the random number r specific to the

transaction and a private key s belonging to an asymmetrical pair of keys[[,]];

[[- 4)]] ~~the chip~~ sending the authentication value V from the chip to the application[[,]]; and

[[- 5)]] verifying, at the application, ~~verifying~~ said authentication value V ~~by means of~~ via a verification function whose input parameters consist ~~exclusively~~ of public parameters including at least ~~the~~ a public key p.

2. (Currently Amended) A The method according to claim 1, wherein producing the random number r specific to the transaction comprises:

[[-]] mixing some or all of the input parameters ~~by means of~~ via a mixing function and supplying a series of bits as ~~the~~ an output of the mixing function[[,]];

[[-]] changing ~~the~~ a state of a finite state automaton from an old state to a new state in accordance with a function depending at least on the old state and a value of the series of bits[[,]]; and

[[-]] determining a series of random bits to form ~~the whole~~ an entire or a portion of the random number r ~~by means of~~ via an output function having input arguments including at least [[a]] the state of the automaton.

3. (Currently Amended) A The method according to claim 2, wherein one input parameter is a ~~secrete~~ secret key K shared by the chip and the application and is stored in a protected memory region of the chip.

4. (Currently Amended) ~~A~~ The method according to claim 1, wherein the mathematical relationship comprises a function g^r in a set G of items g provided with an operation having at least ~~the~~ an associative property of being associative[[.]]

5. (Currently Amended) ~~A~~ The method according to claim 4, wherein the set G is ~~the~~ a group Z_n^* of positive or null integers less than n and prime with n , wherein n is a positive integer.

6. (Currently Amended) ~~A~~ The method according to claim 4, wherein the set G is any elliptical curve constructed on any finite body.

7. (Currently Amended) ~~A~~ The method according to claim 1, wherein the serial function is an arithmetical function executing operations from a list comprising addition, subtraction, and [[left-]] left-shifts or right-shifts.

8. (Currently Amended) ~~A~~ The method according to claim 7, wherein the arithmetical function executes only addition.

9. (Currently Amended) ~~A~~ The method according to claim 7, wherein the arithmetical function executes only subtraction.

10. (Currently Amended) A The method according to claim 7, wherein the arithmetical function input arguments further include input parameters and the arithmetical function entails executing one of the operations $y = r$ and $y = r + s$ as a function of ~~the~~ a value assigned by the application to an input parameter t of the serial function.

11. (Currently Amended) A The method according to claim 10, wherein the mathematical relationship comprises a verification function g^r in a set G of items g provided with an operation having at least an associative ~~the property of being associative~~ and wherein the verification function compares ~~the~~ a result obtained by applying the verification function to the authentication value V with either the value x or the product of the value x and the public key p of the chip corresponding to its secret key s , as a function of the parameter t , which ~~amounts to~~ comprises testing one of the equations $g^y = x$ and $g^y = xp$, as a function of the value of the parameter t , where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the function $p = g^s$.

12. (Currently Amended) A The method according to claim 7, wherein the arithmetical function has, for further input arguments, input parameters and comprises executing the operation $y = r$ or the operation $y = r - s$ as a function of ~~the~~ a value assigned by the application to an input parameter t of the serial function.

13. (Currently Amended) A The method according to claim 12, wherein the mathematical equation comprises a verification function g^r in a set G of items g provided with an operation having at least the property of being associative and wherein the verification function compares

the result obtained by applying the mathematical ~~equation~~ relationship to the authentication value V with the value \underline{x} or with the product of the value \underline{x} and the public key \underline{p} of the chip corresponding to its secret key \underline{s} , as a function of the value of the parameter \underline{t} , which ~~amounts to~~ comprises testing the equation $g^y = x$ or the equation $g^y.p = x$, as a function of the value of the parameter \underline{t} , where \underline{y} is equal to the authentication value V and \underline{p} is the public key of the chip corresponding to its secret key \underline{s} , as defined by the equation $p = g^s$.

14. (Currently Amended) A ~~The~~ The method according to claim 7, wherein the arithmetical ~~function~~ relationship has, for further input arguments, input parameters and comprises executing the operation $y = r + 2^i$ as a function of ~~the~~ a value assigned by the application to an input parameter \underline{t} of the serial function, said parameter \underline{t} comprising a string of \underline{m} bits in which only one bit t_i is equal to 1, \underline{m} being a natural integer.

15. (Currently Amended) A ~~The~~ The method according to claim 14, wherein the mathematical relationship comprises a verification function g^r in a set G of items g provided with an operation having at least an associative ~~the property of being associative~~ and wherein the verification function tests the equation $g^y = x p^{2^i}$, as a function of the value of the parameter \underline{t} , where \underline{y} is equal to the authentication value V and \underline{p} is the public key of the chip corresponding to its secret key \underline{s} , as defined by the function $p = g^s$.

16. (Currently Amended) ~~A~~ The method according to claim 7, wherein the arithmetical function has for₁ further input arguments₁ input parameters and comprises executing the operation $y = r + 2^t s$ as a function of the value assigned by the application to an input parameter t of the serial function.

17. (Currently Amended) ~~A~~ The method according to claim 16, wherein the mathematical relationship comprises a verification function g^r in a set G of items g provided with an operation having at least ~~the~~ an associative property ~~of being associative~~ and wherein the verification function tests the equation $g^y = x p^{2^t}$, as a function of the value of the parameter t , where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the function $p = g^s$.

18. (Currently Amended) ~~A~~ The method according to claim 7, wherein the arithmetical function has₁ for further input arguments₁ input parameters and executes the operation $y = r + t s$ as a function of the value assigned by the application to an input parameter t of the serial function, where t is an integer.

19. (Currently Amended) ~~A~~ The method according to claim 18, wherein the mathematical relationship comprises a verification function g^r in a set G of items g provided with an operation having at least ~~the~~ an associative property ~~of being associative~~ and wherein the verification function compares the result obtained by applying the verification function to the authentication value V with the value x or the product of the value x and the public key p of the chip corresponding to its secret key s , as a function of the value of the parameter t , which ~~amounts to~~

comprises testing the equation $g^y = xp^t$, as a function of the value of the parameter t , where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the function $p = g^s$.

20. (Currently Amended) A The method according to claim 1, wherein the parameter x sent from the chip to the application is ~~the result of~~ a result obtained by applying a hashing function to at least one item linked to the random number r by a mathematical relationship function and to an optional field D containing data linked to the application.

21. (Currently Amended) A The method according to claim 20, wherein the arithmetical function has, for further input arguments, input parameters and executes the operation $y = r + 2^i s$ as a function of the value assigned by the application to an input parameter t of the serial function, said parameter t comprising a string of m bits in which only one bit t_i is equal to 1, where m is a natural integer.

22. (Currently Amended) A The method according to claim 21, wherein the mathematical relationship comprises a verification function g^r in a set G of items g provided with an operation having at least an associative ~~the property of being associative~~ and wherein the verification function tests the ~~equation~~ relationship $h(g^y/p^{2^i}, D) = x$, as a function of the value of the parameter t , where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the function $p = g^s$.

23. (Currently Amended) A The method according to claim 21, wherein the mathematical relationship comprises a verification function g^r in a set G of items g provided with an operation having at least an associative ~~the property of being associative~~ and wherein the verification function tests the ~~equation~~ relationship $h(g^y \cdot p^{2^i}, D) = x$, where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the function $p = g^{-s}$.

24. (Currently Amended) A The method according to claim 20, wherein the arithmetical function has, for further input arguments, input parameters and executes the operation $y = r - 2^i s$ as a function of the value assigned by the application to an input parameter t of the serial function, said parameter t comprising a string of m bits in which only one bit t_i is equal to 1, where m is a natural integer.

25. (Currently Amended) A The method according to claim 24, wherein the mathematical relationship comprises a verification function g^r in a set G of items g provided with an operation having at least ~~the~~ an associative ~~property of being associative~~ and wherein the verification function tests the ~~equation~~ relationship $h(g^y \cdot p^{2^i}, D) = x$, where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the function $p = g^{-s}$.

26. (Currently Amended) ~~A~~ The method according to claim 20, wherein the mathematical function comprises a verification function g^r in a set G of items g provided with an operation having at least ~~the~~ an associative property ~~of being associative~~ and wherein the parameter x sent from the chip to the application is ~~the result of~~ a result obtained by applying a relationship of ~~the type~~ $x = h(g^r, D)$, where D designates an optional field containing data linked to the application and h is the hashing function.

27. (Currently Amended) ~~A~~ The method according to claim 26, wherein the serial function has input arguments ~~in the form of~~ comprised of input parameters and executes either the operation $y = r$ or the operation $y = r + s$ as a function of the value assigned by the application to an input parameter t of the serial function and wherein the verification function compares the value x to the value $h(g^y, D)$ or the value $h(g^y, p, D)$ as a function of the value of the parameter t , where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the equation $p = g^{-s}$.

28. (Currently Amended) ~~A~~ The method according to claim 26, wherein the serial function has, for input arguments, input parameters and executes ~~either one of~~ either one of the operation $y = r$ ~~or~~ and the operation $y = r + s$ as a function of the value assigned by the application to an input parameter t of the serial function and wherein the verification function compares the value x to the value $h(g^y, D)$ or the value $h(g^y, p, D)$ as a function of the value of the parameter t , where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the equation $p = g^{-s}$.

29. (Currently Amended) A ~~The~~ method according to claim 26, wherein the serial function has, for input arguments, input parameters and executes ~~either one of~~ the operation $y = r$ ~~or~~ and the operation $y = r - s$ as a function of the value assigned by the application to an input parameter t of the serial function and wherein the verification function compares the value x to the value $h(g^y, D)$ or the value $h(g^y.p, D)$ as a function of the value of the parameter t , where y is equal to the authentication value V and p is the public key of the chip corresponding to its secret key s , as defined by the equation $p = g^s$.

30. (Currently Amended) A ~~The~~ method according to claim 7, wherein the set G is the group Z_n^* of positive or null integers less than n and prime with n .

31. (Currently Amended) A ~~The~~ method according to claim 7, wherein the set G is any elliptical curve constructed on any finite body.

32. (Currently Amended) A device including an electronic chip ~~according to claim 1~~ and ~~adapted~~ configured to implement an asymmetrical cryptographic method ~~of~~ for protecting the electronic chip against fraud in transactions between the electronic chip and an application, said chip reading one or more stored values of a parameter x calculated prior to a transaction by the application, and said parameter x being linked by a mathematical relationship to a value of a random number r , the method comprising the electronic chip calculating an authentication value V from input parameters, and said device comprising:

[[-]] a serial pseudo-random generator for producing a random number r
specific to the transaction[[,]];

[[-]] first memory means for storing the one or more values of the parameter x calculated prior to the transaction by the application ~~and~~ which are linked by [[a]] the mathematical relationship to the value of the random number r[[,]];

[[-]] means for sending the parameter x linked to the random number r specific to the transaction from the chip to the application[[,]];

[[-]] means for executing a serial function having as input parameters at least the random number r specific to the transaction and a private key s belonging to an asymmetrical pair of keys and providing as output a parameter y[[,]]; and

[[-]] output means ~~adapted~~ configured to construct ~~the~~ an authentication value V from at least the parameter y.

33. (Currently Amended) A verification device for executing an asymmetrical cryptographic method ~~of~~ for protecting an electronic chip ~~according to claim 1~~ against fraud in transactions between the electronic chip and an application, said chip reading one or more stored values of a parameter x calculated prior to a transaction by the application, and said parameter x being linked by a mathematical relationship to a value of a random number r, said method comprising verifying an authentication value V calculated by the electronic chip from exclusively public parameters and said verification device comprising means for executing the verification function ~~taking as~~ based on input which comprises at least the authentication value V and ~~the~~ a public key p.